

Exponential Distribution (3)

- Memoryless/Markov property
 - The future is independent of the past!
 - The remaining lifetime of a component, which functions at time t , is independent of t

$$\begin{aligned}R(h | t) &= P\{T > t + h | T > t\} \\ &= P\{T > h\} = R(h) \quad \forall t, h > 0\end{aligned}$$

$$\begin{aligned}P\{T > t + h | T > t\} &= \frac{P\{T > t + h \cap T > t\}}{P\{T > t\}} \\ &= \frac{P\{T > t + h\}}{P\{T > t\}} = \frac{e^{-\lambda(t+h)}}{e^{-\lambda t}} \\ &= e^{-\lambda h} = P\{T > h\}\end{aligned}$$