

ECE454/544 Extra-Credit Question (Fall 2022)

A machine with constant failure rate  $\lambda$  will survive a period of 200 hours without failure, with the probability of 0.97.

- Determine the failure rate  $\lambda$
- Find the mean time to failure (MTTF) of the machine
- Find the probability that the machine will survive 1000 hours without failure

$$\begin{aligned} \textcircled{1} \quad e^{-\lambda t} &= 0.97 & e^{-\lambda \cdot 200} &= 0.97 \\ -\lambda \cdot 200 &= \ln 0.97 & & \textcircled{3} \\ \lambda &= \frac{-\ln 0.97}{200} = 0.000152296 \end{aligned}$$

$$\textcircled{2} \quad \text{MTTF} = \frac{1}{\lambda} = 6566 \text{ hrs} \quad \textcircled{1}$$

$$\begin{aligned} \textcircled{3} \quad e^{-\lambda t} &= e^{-0.000152296 \cdot 1000} \\ &= 0.858734. \quad \textcircled{2} \end{aligned}$$