

Department of Electrical and Computer Engineering  
University of Massachusetts Dartmouth

ECE544 Fault-Tolerant Computing  
& Reliability Engineering

Fall 2022

Homework #7

Name: \_\_\_\_\_

Instructor: Prof. Liudong Xing

**ECE544: Fault-Tolerant Computing & Reliability Engineering (Fall 2022)**  
**Homework #7**

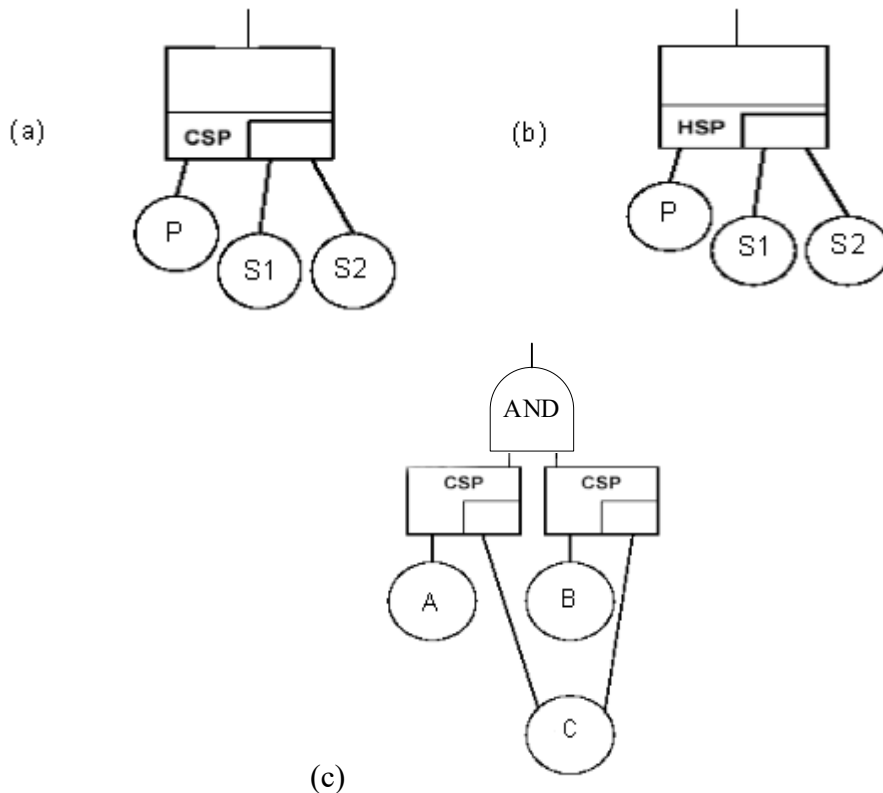
**Assigned:** November 14, Monday  
**Due:** November 21, Monday

**Instructions:**

1. Please type your answers or write your answers clearly (illegible writing will NOT be graded).
2. Show all steps of your solution. Answers without justification would subject to a big penalty.
3. Please organize all pages of your answers into one file, name your file using **“HW7-your last name.pdf or doc”** (e.g., HW7-Xing.pdf), and submit it to [lxing@umassd.edu](mailto:lxing@umassd.edu) electronically or submit a hard copy by the due date
4. Relevant lectures: **L#14, L#15**

**Problems:**

1. Consider the three dynamic fault trees in the following figure. Assume each component  $i$  has an exponential time-to-failure distribution with parameter  $\lambda_i$ , where  $i = P, S1, S2, A, B, C$ . For example, component A has failure rate of  $\lambda_A$ . Generate the Markov chain model (i.e., the state transition diagram) of each fault tree.



2. For the fault tree model below, assume components A and B have the failure rate of  $\lambda_A$  and  $\lambda_B$ , respectively. Component C has the failure rate of  $\lambda_C$  after being activated to replace a failed primary component.

- a) find the state transition diagram of the Markov chain
- b) find the state equations for the **time-dependent** solution
- c) find the state equations of the **asymptotic** solution
- d) find the system unreliability in the **steady-state** by solving the state equations in part c)

